

# **CSS Past Paper**

# Applied Mathematics

(2020)

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### FEDERAL PUBLIC SERVICE COMMISSION COMPETITIVE EXAMINATION-2020 FOR RECRUITMENT TO POSTS IN BS-17 UNDER THE FEDERAL GOVERNMENT

**Roll Number** 

## **APPLIED MATHEMATICS**

### TIME ALLOWED: THREE HOURS

**MAXIMUM MARKS = 100** 

NOTE:(i) Attempt ONLY FIVE questions. ALL questions carry EQUAL marks

- (ii) All the parts (if any) of each Question must be attempted at one place instead of at different places.
- (iii) Candidate must write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.
- (iv) No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
- (v) Extra attempt of any question or any part of the attempted question will not be considered.
- (vi) Use of Calculator is allowed.

**Q. No. 1.** (a) Prove that 
$$\nabla^2 r^n = n(n+1)r^{n-2}$$
 (10)

(b) Evaluate 
$$\iint_{s} \underline{A} \cdot \overline{n} \, ds$$
 where  $\overline{A} = 18 \, \underline{z} \, \underline{i} - 12 \, \underline{j} + 3y \, \underline{k}$  and S is that part of the plane (10)  $2x + 3y + 6z = 12$  which is located in the 1<sup>st</sup> octant.

- **Q. No. 2.** A particle P of mass m slides down a frictionless inclined plane AB of an angle  $\alpha$  with the horizontal. If it starts from rest at the top A, find (a) the acceleration (b) the velocity and (c) the distance travelled after time t.
- Q. No. 3. (a) Discuss the motion of a particle moving in a straight line if it starts from rest at a distance 'a' from a point O and moves with an acceleration equal to k times its distance from O.
  - (b) Find radial and transversal components of velocity and acceleration. (10)

**Q. No. 4.** (a) Solve 
$$\frac{d^2y}{dx^2} + y = Co\sec x$$
 (10)

**(b)** Solve 
$$dy + \frac{y - Sinx}{x} dx = 0$$

Q. No. 5. (a) Solve the initial value problem 
$$x(2+x)\frac{dy}{dx} + 2(1+x)y = 1 + 3x^{2}, \quad y(-1) = 1$$

(b) Find the general solution of the equation 
$$(D^3 - 2D + 1)y = 2x^3 - 3x^2 + 4x + 5$$
 (10)

Q. No. 6. (a) Find the Fourier series of f: 
$$f(x) = \begin{cases} x, 0 < x < 1 \\ 0, 1 < x < 2 \end{cases}$$
 (10)

(b) Solve the boundary value problem 
$$\frac{\partial^2 u}{\partial x^2} = \frac{1}{k} \frac{\partial u}{\partial t}$$
  
Satisfying  $u(0,t)=u(1,t)=0$  and  $u(x,0)=1x-x^2$ 

### **APPLIED MATHEMATICS**

- Q. No. 7. (a) By using regular Falsi method, solve Logx Cosx = 0 (10)
  - (b) Find the value of f(7.5) by using Newton Gregory Backward Difference Interpolation formula. X: 5, 6.1, 6.9, 8, 8.6 f(x): 3.49, 4.82, 5.96, 7.5, 8.2
- Q. No. 8. (a) Applying the Taylor series method, compute  $\int_{0}^{x} \frac{Sin t}{t} dt \text{ for } x = 0 \text{ (0.1)1}$ 
  - (b) Use fourth order RK method to solve  $\frac{dy}{dx} = t + y \; ; \; y(0) = 1 \; from \; t = 0 \; to \; t = 0.4 \; taking \; h = 0.4$

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