

# CSS Past Paper **Statistics**(2019)

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# FEDERAL PUBLIC SERVICE COMMISSION COMPETITIVE EXAMINATION-2019 FOR RECRUITMENT TO POSTS IN BS-17 UNDER THE FEDERAL GOVERNMENT

Roll Number

(20)

## **STATISTICS**

TIME ALLOWED	: THREE HOURS	PART-I (MCQS)	MAXIMUM MARKS = 20
<b>PART-I(MCQS):</b>	MAXIMUM 30 MINUTES	PART-II	MAXIMUM MARKS = 80

NOTE: (i) Part-II is to be attempted on the separate Answer Book.

- (ii) Attempt ONLY FOUR questions from PART-II by selecting TWO questions from EACH SECTION. ALL questions carry EQUAL marks.
- (iii) All the parts (if any) of each Question must be attempted at one place instead of at different places.
- (iv) Write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.
- (v) No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
- (vi) Extra attempt of any question or any part of the question will not be considered.
- (vii) Use of Calculator is allowed.

# <u>PART – II</u> <u>SECTION – I</u>

- Q. 2. (a) What is meant by a frequency distribution? Describe briefly the main steps in the (6) preparation of a frequency table from raw data.
  - (b) A man travels from A to B at average speed of 30 miles per hour and returns from B to A along the same route at an average speed of 60 miles per hour. Find the average speed of the entire journey.
  - (c) Define mean-deviation and its co-efficient. Discuss its advantages and uses.

    Estimate the mean deviation from the arithmetic mean of the following set of examination marks.

Marks	0-9	10-19	20-29	30-39	40-49	50-59	60-69	70-79
No. of	2	3	8	24	27	40	11	5
students								

- Q. 3. (a) Define mutually exclusive events. State and prove the theorem of addition of (6) probabilities concerning mutually exclusive events.
  - (b) Show that the multiplication law  $P(A \land B)=P(A/B)P(B)$ , established for two events, may be generalized to three events as follows;

$$P(A \land B \land C) = P(A/B \land C) P(B/C) P(C)$$

- (c) There are three coins, identical in appearance, one of which is ideal and the other two biased with probabilities 1/3 and 2/3 respectively for a head. One coin is taken at random and tossed twice. If a head appears both the times, what is the probability that the ideal coin was chosen?
- Q. 4. (a) (i) Explain briefly how the principle of least squares is used to find a regression (6) line based on a sample of size n. Illustrate on a rough sketch the distance whose squares are minimized, taking care to distinguish the dependent and independent variables.
  - (ii) Find the least square estimates of parameters in a simple linear regression model  $Y_i = \alpha + \beta X_i + e_i$  where  $e_i$ 's are distributed independently with mean zero and constant variance.
  - (iii) What are the properties of least square regression line?
  - **(b)** The following means, standard deviations and correlations are found for (6)

 $X_1$  = Seed-hay crops in owts. Per acre

 $X_2$  = Spring rainfall in inches

 $X_3$  = Accumulated temperature above  $42^{\circ}$  F in spring in a certain district in England during 20 years.

$$egin{aligned} ar{X}_1 &= 28.02, & S_1 &= 4.42, & r_{12} &= 0.80, \\ ar{X}_2 &= 4.91, & S_2 &= 1.10, & r_{13} &= -0.40, \\ ar{X}_3 &= 594, & S_3 &= 85, & r_{12} &= -0.56, \end{aligned}$$

Find the partial correlation and the regression equation for hay-crop on spring rainfall and accumulated temperature.

# **STATISTICS**

(c) What do you understand by nonparametric tests? Why such tests are also called (8) distribution-free tests? Give the advantages and disadvantages of nonparametric tests over parametric tests. Describe the Wilcoxon signed-rank test for one sample. How does it differ from the sign test?

## **SECTION-II**

- **Q. 5.** (a) Explain what you understand by the probability sampling and non probability (6) sampling. What are their relative advantages and disadvantages?
  - **(b)** What is a sampling distribution? Describe the properties of the sampling distribution (6) of the means.
  - (c) A finite population consists of the numbers 2, 4 and 6. Form a sampling distribution (8) of sample mean, when random samples of size 4 is drawn with replacement. Also verify its properties.
- Q. 6. (a) Under what condition is the sampling distribution of  $\frac{s_1^2}{s_2^2}$  an F-distribution? Explain the relationship between the F and t distributions, between the F and Chi-Square distributions.
  - The proportion of families buying milk from company A in a certain city is believed to be p=0.6. If a random sample of 10 families shows that 3 or less buy milk from company A, we shall reject the hypothesis that p=0.6 in favour of the alternative p<0.6. Evaluate  $\alpha$  if p=0.6, evaluate  $\beta$  for the alternatives p=0.3, p=0.4 and p=0.5.
  - (c) Define a Chi-square random variable and its density function. Discuss the important (8) properties of Chi-square distribution. Show that the Chi-square distribution tends to normal distribution for large degrees of freedom.
- Q. 7. (a) Describe the Randomized Complete Block Design, its model and analysis. What are (6) its advantages and disadvantages?
  - (b) Compare Randomized Complete Block experiments with Completely Randomized (6) experiments, comparing their respective advantages and relative efficiency, with illustrations.
  - (c) Three varieties A, B and C of a crop are tested in a randomized block design with four (8) replications, the layout being given below. The plot yields in pounds are also indicated therein. Analyze the experimental yields and state your conclusions.

	1	A 32.1	C 34.2	B 31.7
Replications	2	C 30.7	A 17.0	B 32.7
	3	A 40.8	B 25.3	C 48.2
	4	B 47.9	C 59.6	A 26.8

- Q. 8. (a) Define gross and net production rates. Explain how would you compute the net (6) production rate and what interpretations can be made if it is 1, less than 1 or greater than 1.
  - **(b)** Explain with suitable illustrations the object of standardizing various vital statistics (6) relating to births, deaths and marriages.
  - (c) Compute the gross and net reproduction rates for the following data: (8)

Age-group	Female	Female	Probability
(years)	Population (000)	births	of survival
15-19	1558	18900	0.914
20-24	1112	71100	0.899
25-29	1595	96900	0.884
30-34	1629	64200	0.868
35-39	1627	34900	0.852
40-44	1522	10800	0.834
45-49	1401	800	0.813

